

C 40931

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Name.....

Reg. No.....

**FOURTH SEMESTER B.TECH. (ENGINEERING) DEGREE EXAMINATION
APRIL 2013**

EN 09 401 B—ENGINEERING MATHEMATICS IV

(2009 Admissions—Regular/Supplementary/Improvement)

[Common for IC, EC, EE, AI, BM, SC and IT]

Time : Three Hours

Maximum : 70 Marks

Part A

Answer all questions.

1. If X follows the uniform distribution in $(-K, K)$ find K such that $P(X > 1) = \frac{1}{3}$.
2. Find the Z-transform of n^2 .
3. Show $P_n(1) = 1$.
4. Solve $\sqrt{p} + \sqrt{q} = 1$.
5. Solve $(pq - p - q)(z - px - 9y) = pq$.

(5 × 2 = 10 marks)

Part B

Answer any four questions.

1. The probability that a bomb dropped from a plane will strike the target is 0.2. If 6 bombs are dropped find the probability that (a) exactly two will strike the target. (b) at least two will strike the target. (c) at most two will strike the target.
2. The probability of hitting an aircraft is 0.001 for each shot. How many shots should be fired so that the probability of hitting with two or more shots is above 0.95 ?
3. Solve $u_{k+1} + u_k = 1$ if $u_0 = 0$ using Z-transforms.
4. Prove that $\frac{d}{dx} (x^{-n} J_n(x)) = -x^{-n} J_{n+1}(x)$.

Turn over

5. Solve $z^2(p^2 + q^2 + 1) = a^2$.
6. Solve $(x^2 - y^2 - z^2)p + 2xyq = 2xz$.

(4 × 5 = 20 marks)

Part C*Answer all questions.*

1. At an examination, 10% of the students got less than 30 marks and 97% got less than 62 marks. Assuming normal distribution, find μ and σ . Find the percentage of students who got marks between 40 and 70.

Or

2. Define the following distributions : (a) Geometric distribution. (b) Hyper geometric distribution. (c) Gamma distribution and (d) Uniform distribution.

3. Find the inverse z -transform of $\frac{z^2 + 3}{(z - 1)(z^2 + 1)}$ by Residue method.

Or

4. Find the inverse z -transform of $\frac{10z}{z^2 - 3z + 2}$ by long division method.

5. Prove that $(1 - 2xz + z^2)^{-1/2} = \sum_{n=0}^{\infty} P_n(x)z^n$.

Or

6. Prove that $J_{-n}(x) = (-1)^n J_n(x)$.

7. Derive the one dimensional heat equation.

Or

8. Obtain the D'Alembert's solution of the one dimensional wave equation.

(4 × 10 = 40 marks)